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CORRELATING BULK DENSITY (WITH DOCKAGE) AND TEST WEIGHT (WITHOUT DOCKAGE) FOR WHEAT SAMPLES

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ABSTRACT. *In grain bins, the compaction of stored grain is caused by the overbearing pressure of the bulk material in the bin. To predict the amount of grain in the bin, compaction values must be determined based on the average bulk density (BD) of the stored material. However, BD is determined following the Federal Grain Inspection Service (FGIS) guidelines for measuring test weight (TW), which require that dockage be removed prior to measuring wheat TW. Thus, this creates a problem for predicting grain compaction and conducting inventory studies, because the average BD of the grain in a bin for these calculations should include dockage. Therefore, regression models between the TW without dockage and the BD with dockage were obtained based on the reported scale data during wheat harvest from three elevators located in Kansas and Oklahoma. A power model was used to predict BD with dockage when TW without dockage and dockage levels are given. Laboratory samples of HRW and SRW wheat with dockage levels ranging from 0.05% to 5% showed a second order polynomial trend when plotted against decrease in BD with dockage values compared to TW without dockage. These results will be crucial for determining grain packing inventory parameters for HRW wheat bins.*

Keywords. *Dockage, HRW, SRW, Stored grain inventory, Test weight, Wheat.*

Agricultural grains such as wheat, corn, and soybeans are compressible materials and, in storage, they are affected by pressure from overbearing loads. However, the degree of compressibility of stored grain varies with grain type, grain properties, and the geometry of the bin in which the grain is stored. Several studies have investigated the compressibil-

ity of a variety of food crops, such as ground shelled corn, wheat, corn, soybean, corn meal, sugar beet pulp, cotton seed meal, and distillers grains without solubles (Loewer et al., 1977; Malm and Backer, 1985; Bhadra et al., 2015; Boac et al., 2015). Milani et al. (2000) determined that the effects of pressure and moisture on bulk densities of soybean were independent of variety). Additional studies have been conducted related to the effect of grain spreaders on the bulk density (BD) of stored wheat, yellow corn, and sorghum (Chang et al., 1981) and different methods of transfer, such as choke fed and non-choke fed through an orifice (Chang et al., 1983).

Janssen's (1895) equation is commonly used to predict the vertical and lateral pressures in bins and is based on the BD of the stored material, coefficient of friction, lateral to vertical pressure coefficient and the bin geometry. Studies have also been conducted in which the degree of compressibility or packing of grain in bins has been estimated using the differential form of Janssen's equation (Thompson and Ross, 1983; Thompson et al., 1987; McNeill et al., 2008). Grain packing models based on this form of Janssen's equation were adopted as an ASAE standard in 1992 and later revised in 2010 (ASABE Standards as EP413.2, 2010, R2014).

Inventory control of stored grain is extremely important for farmers, elevator managers, and bin designers and is crucial for the grain bin managers, who must track the quantity of the crop and meet federal and state regulatory obligations. Each truck load of grain stored in a bin is sampled and quality parameters measured following standards in the USDA Federal Grain Inspection Service

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(FGIS) Handbook (USDA-GIPSA, 2009). Official inspection of grain by a state or federal regulatory body can only be conducted using FGIS-approved equipment and procedures. For wheat, the moisture content, dockage, TW, and percent of shrunken and broken kernels are the most important extrinsic parameters measured as per FGIS guidelines.

When grain is delivered to elevators, samples of wheat, including Hard Red Winter (HRW) and Soft Red Winter (SRW) classes, are taken from incoming trucks or trailers using mechanical probes. These samples are evaluated for moisture content before the removal of dockage, and evaluated for TW after the dockage has been removed (USDA-GIPSA, 2009). Dockage is the material other than the predominant grain that can easily be removed with sieves and cleaning devices, the detailed definition is given in the Materials and Methods section.

Test weight is defined as the weight of the volume of grain that is required to fill a Winchester bushel ($2,150.42 \text{ in.}^3$) to capacity (USDA-GIPSA, 2009). The unit of TW is then lb/bu. Thus, the TW measures the BD under specific conditions (Bern and Brumm, 2009) including, in the case of wheat, that the dockage has been removed. This standard procedure of removing the dockage before TW evaluation creates a problem for grain packing models. The models need BD with dockage as an input to calculate grain packing. The BD without dockage, measured as per the FGIS guidelines, will be denoted as test weight (TW) throughout this article, following the grain industry norm. This will be distinguished from bulk density with dockage, measured with the same device. There is no data in the literature on the relationship between TW (without dockage) and BD with dockage for wheat. Furthermore, field-observed dockage levels are commonly less than 1%, but can range higher under rare scenarios. Hence, it would be useful to determine the effects of dockage levels of up to 5% to include the extreme levels and to evaluate correlation trends, which should be clearer with the inclusion of higher dockage levels. Thus, the objectives of this research were to: (1) develop a regression model for predicting the BD with dockage from the FGIS-measured TW and the FGIS-measured dockage values in the field and (2) evaluate the effect of dockage on the BD of wheat samples for dockage levels up to 5%. Samples at above 1% dockage cannot be readily obtained from the field and will need to be prepared in the laboratory.

MATERIALS AND METHODS

TEST WEIGHT DATA COLLECTION

The FGIS-approved TW apparatus consists of a hopper discharge container with a slide gate and a one dry quart cup (Seedburo Equipment, Chicago, Ill.). The weight of grain in the quart cup is measured in pounds and is multiplied by 32 (number of dry quarts in a Winchester bushel) to obtain the TW in pounds per bushel (lb/bu) as described in the handbook (USDA-GIPSA, 2009). According to FGIS standards, the minimum TW per bushel for HRW wheat should range from 51.0 to 60.0 lb/bu for all

U.S. wheat grades No. 1 to No. 5 (Matz, 1991) with the standard bushel weight of one bushel of wheat equal to 60 lb.

TW data for HRW wheat were collected from three different elevators located in northeast Kansas (Manhattan, Kan.), northern Oklahoma (Enid, Okla.), and western Kansas (Goodland, Kan.) during wheat harvest season in 2011 and 2013. Trucks were sampled as they arrived at the scale and sample test weights without dockage, following FGIS procedures, were obtained directly from scale data reports from the elevator managers. FGIS standards (USDA-GIPSA, 2009) define dockage primarily as the foreign material that is lighter, larger, or smaller than grain. Also, it is the underdeveloped shriveled and small pieces of wheat kernels that is removed from separated wheat, but cannot be recovered by properly rescreening or recleaning. The unthreshed kernels that pass over the riddle (in the Carter dockage tester) are also considered dockage.

A moisture content analysis was also performed for those samples. The moisture content of the field samples ranged from 10.0% to 12.9% (wb), with an average of 11.5% (wb). Before discarding the samples from each truck, dockage and cleaned grain from the sample were mixed together uniformly and the resulting BD (with dockage) was measured. Thus, TW (without dockage), BD (with dockage), and moisture content were measured from the same sample from each truck load.

Separate clean wheat samples were procured from four states in the United States (Kansas, Kentucky, Oklahoma, and Texas) and mixed with dockage from a commercial flour mill at varying levels ranging from 0.05% to 5% by weight for laboratory tests to determine the BD. This part of the dataset was used in the second part of the analysis where we determined the change in BD with dockage levels. Since field samples only rarely have more than 1% dockage it was necessary to prepare laboratory samples with these higher dockage levels. The wheat samples from Kansas, Oklahoma, and Texas were HRW wheat, while the wheat sample from Kentucky was SRW wheat. The moisture contents for the laboratory wheat samples ranged from 8.8% to 13.3% (wb). Lab samples with the discrete dockage levels were compared to the field samples after grouping the field samples by dockage level in 0.1% increments. Based on the observed standard deviations, and the z-value for a 5% margin of error, the minimum number of observations should be 20, so the field samples were grouped in 0.1% increments for cases where at least 20 observations were in the dataset. The lab samples (sample size of 3 kg) were also split into three 1 kg subsamples. Each subsample had TW measurements repeated for 10 times, yielding 30 total measurements, for each dockage level.

DATA ANALYSIS

The measured decrease in BD with dockage when compared to TW values was plotted and analyzed for each dockage level. A statistical analysis was performed using both single and multiple regression techniques for correlating BD (with dockage) with TW (without dockage).

The single regression analysis was performed using Microsoft Excel 2007 (Redmond, Wash.), and samples were classified based on 4 different dockage levels: 0% to 0.39%, 0.4% to 0.59%, 0.6% to 0.9%, and 1% and above. The multiple regression analysis was performed using CurveExpert Professional software (version 2.0.3, 2013) to predict BD with dockage as a function of dockage level and TW without dockage.

Multiple regression models for predicting BD with dockage as a function of TW and dockage level were evaluated using CurveExpert Professional software. Since a true R^2 does not exist for the nonlinear models, standard error and the Akaike Information Criterion (AIC) were used to select the best model. AIC is a statistical parameter that strikes a balance between the goodness of fit of a model and the complexity of the model (Akaike, 1974):

$$AIC = 2k - 2\ln(L) \quad (1)$$

where

k = number of parameters in the statistical model.

L = maximized value of the likelihood function of the estimated model.

The preferred model will have the lowest AIC value. This technique includes a penalty prediction that discourages any increase in the number of parameters that can lead to overfitting and a higher goodness of fit (Fang, 2011).

RESULTS AND DISCUSSION

All field data (Enid, Okla.; Manhattan, Kan.; and Goodland, Kan.) are shown in figure 1 with BD with dockage as a linear function of TW (without dockage). The simple linear model (no intercept) had a slope of 0.986 and an R^2 of 0.724. In this raw plot the effect of varying levels of dockage only appears as scatter. The Goodland data show by far the greatest scatter of the three locations in figure 1, apparently caused by high dockage levels observed during an unusually rainy harvest season in 2011 (dockage in the Goodland samples ranged up to 3% compared to a maximum of 1% for the other two locations). A simple linear model without the Goodland data had a slope of 0.992 and an R^2 of 0.886. Neither of these correlations include the level of dockage as an independent variable.

MULTIPLE REGRESSION

Table 1 shows the best three models from the multiple regression analysis along with two simple linear correlations between BD and TW. Numerous other non-linear models were evaluated with CurveExpert Pro but they did not produce as good fit as these three. Power Model 1 yielded the least AIC value of -258 and near the best standard error value at 0.880. For these models similar standard errors indicate that the differences between predictions were small. Both the Two-Variable Linear Model and Power Model C (table 1) suffer from a discontinuity at dockage = 0%. However, in this case TW

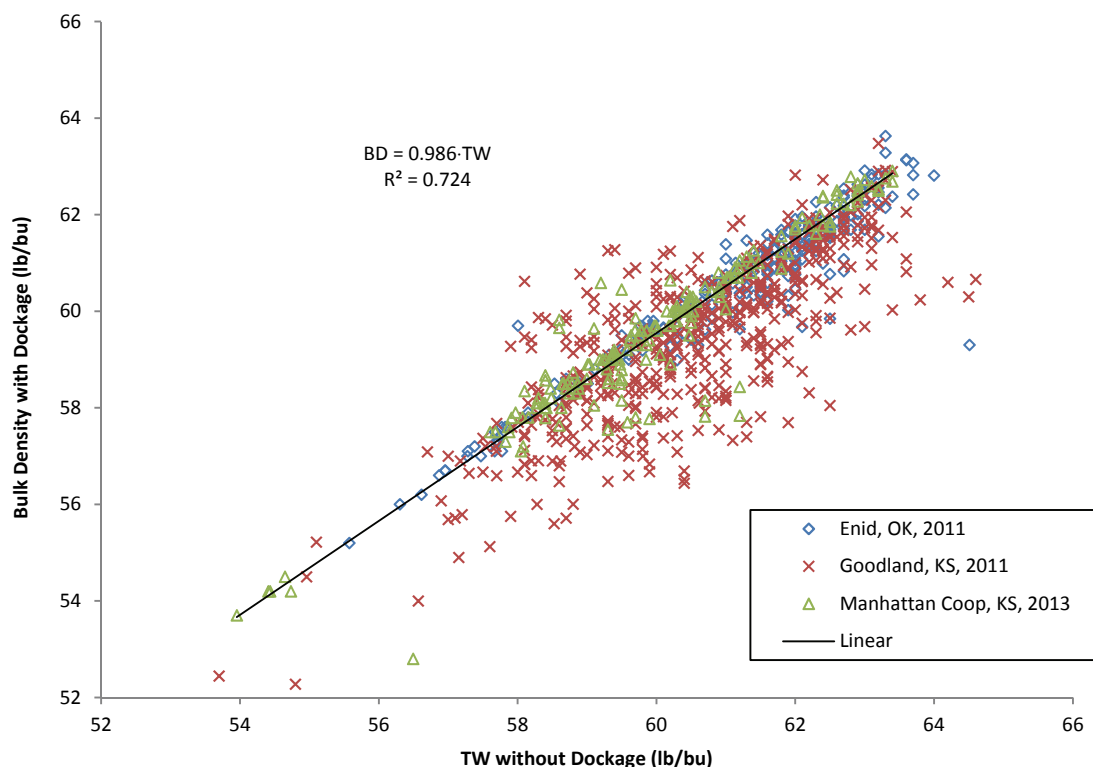


Figure 1. Bulk density vs. test weight of HRW wheat samples with dockage from 0% to 3.6%.

Table 1. Selected models for predicting bulk density with dockage from test weight and dockage level.^[a]

Model Name	Model Structure	AIC	Std Error (lb/bu)	Parameter Estimates			
				a	b	c	d
Single-Variable Models, $BD = f(TW)$							
Simple Linear	$BD = a(TW)$	-172.3	0.915	0.986			
1-Variable Linear	$BD = a + b(TW)$	-211.9	0.896	6.66	0.876		
Two-Variable Models, $BD = f(TW, dk)$							
Power Model C	$BD = a(dk)^b + c(TW)^d$	-253.8	0.877	-0.680	0.443	1.470	0.904
2-Variable Linear	$BD = a + b(dk) + c(TW)$	-246.7	0.880	6.10	-0.365	0.889	
Power Model 1	$BD = TW + (dk^b)(a(TW) + c)$	-257.9	0.880	-0.120	0.260	5.890	

^[a] AIC is the Akaike Information Criterion; Std error is the statistical standard error; a to d are the model parameter estimates; dk (dockage level, %) and TW (Test weight, without dockage, lb/bu) are the two independent variables in the listed models; BD (bulk density with dockage) (lb/bu) is the dependent variable. At dockage = 0%, TW without dockage is same as BD with dockage; Bold font indicates final selected model.

without dockage should be exactly equal to BD with dockage, but these two models cannot handle 0% dockage properly. Thus, Power Model 1 (table 1) was selected as the best model for predicting BD with dockage from TW (without dockage) and level of dockage. The single-variable models (BD as a function of TW only) in table 1 and figure 1 did not have any problem with 0% dockage, but neither model had as low a standard error value as the two-variable models.

The greater scatter in the Goodland data was evaluated using a cross validation statistical analysis, following the procedure in Casada and Armstrong (2009). This analysis used a correlation equation which included dockage as an independent variable and showed (table 2) the expected high standard error from the Goodland data. The Goodland data was also poorly predicted ($SEP = 1.12$ lb/bu) by the calibration from the other two locations compared to the predictions ($SEP < 0.7$ lb/bu) of the other two individual locations when they were left out of the calibrations. These results indicate that the correlation from the entire dataset is required to predict BD with dockage from TW (without dockage) for poor quality, high-dockage samples (dockage levels above 1.0%) like those in the Goodland data. For a normal harvest and normal dockage levels (dockage levels below 1.0%) a limited correlation from only the two locations with normal dockage levels could probably be used. Such a correlation from only two locations with

normal harvest conditions would lack robustness and was not pursued further.

LABORATORY STUDY

The greatest scatter in the field data occurred with the Goodland, Kansas samples, which often had unusually high dockage values (up to 3%) that are rare for field data. The effect of high dockage levels (above 1%) was not clear from the limited examples in the field data, so these effects were further evaluated with separate, initially clean wheat samples from four states that were mixed with dockage at levels from 0.05% to 5% under normal laboratory conditions. The highest dockage of 5% was included to clarify dockage effects even though this was even higher than the highest dockage level found in the field data. BD with dockage was lower than TW without dockage because dockage is a lighter material than wheat kernels, which in turn lowers the BD. Also, the presence of the dockage material may have reduced the compaction of the whole wheat kernels. The difference between the BD and TW values was calculated for each sample and this decrease in BD caused by dockage was plotted as a function of dockage level (fig. 2). The plot showed a non-linear trend that was fit using a second order polynomial.

Based on the observed standard deviations, and using the z-value for a 5% margin of error, the minimum number of observations should be 20. Figure 2 shows the field samples, grouped by dockage level in 0.1% increments, when there were at least 20 observations. This minimum of 20 observations eliminated the high dockage level readings, mostly from the Goodland data, and all the field data in figure 2 had dockage levels below 0.75%. According to the FGIS handbook (USDA-GIPSA, 2009), any dockage between 0% and 0.1%, should be reported as 0%. The average of cases with 0% dockage did not show BD with dockage equal to TW values, apparently because there was, on average, 0.05% dockage in those samples. Hence, for field data in figure 2 the dockage level that was reported as 0% is shown as 0.05%, assuming 0.05% was the average dockage for samples between 0% and 0.1%.

Figure 2 shows that the relationship between the decrease in BD and dockage level is nonlinear, with each of

Table 2. Cross-validation results: standard errors for TW from three locations.^[a]

Locations Included	Location Left Out	Standard Errors (lb/bu) ^[b]		
		SEC	SEP	SE _{location}
Enid & Goodland	Manhattan	0.93	0.68	0.61 (SE _{Manhattan})
Enid & Manhattan	Goodland	0.54	1.12	0.80 (SE _{Goodland})
Goodland & Manhattan	Enid	0.97	0.61	0.61 (SE _{Enid})
Average:		0.81	0.81	0.67

^[a] Model: $BD = TW + (dk)^b(a \cdot TW + c)$, please refer to table 2 for model details.

BD = bulk density w/ dockage, lb/bu; TW = test weight, lb/bu; dk = dockage, %.

^[b] SEC = standard error of calibration from combined data from two locations.

SEP = standard error of prediction for the location that was left out.

SE_{location} = standard error for the single location (denoted by the subscript) left out.

the second order polynomial having a goodness of fit (R^2) greater than 0.97 and SEM values ranging from 3.07E-03 to 6.79E-03. The R^2 values were used to compare these regression models because the coefficients were fit by linear regression (Steel and Torri, 1980). The apparent linear trend seen in the field data in figure 1 may have been because the effect of dockage level was not included (other than causing scatter) in the relationship in that figure. However, the broader range of dockage levels used in laboratory samples may have made the polynomial relationship more noticeable in figure 2 than it was with the narrow range of dockage in the field samples.

CONCLUSIONS

Predicting grain compaction requires knowledge of the BD with dockage; however, FGIS guidelines specify the TW for wheat is measured without dockage. These results allow the prediction of BD with dockage when dockage level and TW are known.

The following conclusions were drawn from this research:

1. Power Model 1 was selected as the best model for predicting BD with dockage from TW (without dockage) and level of dockage for HRW wheat field

samples. The model was developed over the moisture range 10.0% to 12.9% (wb) and dockage levels of 0% to 3.2%.

2. Bulk density decrease caused by dockage is related to TW without dockage by a second order polynomial model that was developed over the range of 0.05% to 5% dockage, for both field and laboratory wheat samples consisting of HRW and SRW wheat classes.
3. The moisture range for all the wheat samples (including field and laboratory samples) in this study were from 8.8% to 13.3% (wb) and no significant correlation between BD and moisture levels of the samples in that range was found.

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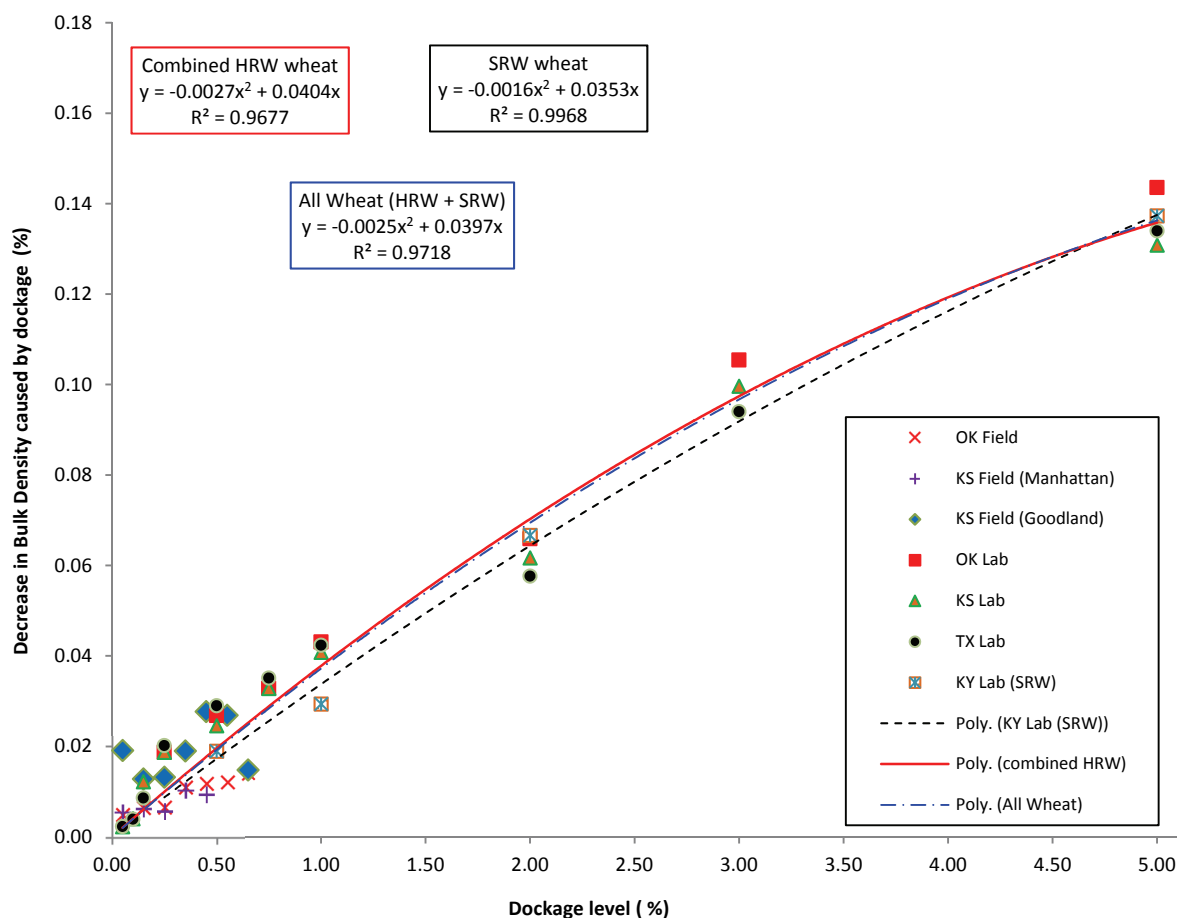


Figure 2. Decrease in bulk density due to dockage (%) vs. dockage level (%) for wheat samples from field and laboratory studies, with best fit polynomial curves for the HRW, SRW, and combined wheat samples.

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REFERENCES

- Akaike, H. (1974). A new look at the statistical model identification. *IEEE Trans. Automatic Control*, 19(6), 716-723. <http://dx.doi.org/10.1109/TAC.1974.1100705>
- ASABE Standards. (2010). EP413.2: Procedure for establishing volumetric capacities of cylindrical bins. St. Joseph, MI: ASABE.
- Bern, C., & Brumm, T. J. (2009). Grain test weight deception. Ames: University Extension, Iowa State University. Retrieved from <http://www.extension.iastate.edu/publications/pmr1005.pdf>
- Bhadra, R., Turner, A. P., Casada, M. E., Montross, M. D., Thompson, S. A., Boac, J. M., ... Maghirang, R. G. (2015). Pack factor measurements for corn in grain storage bins. *Trans. ASABE*, 58(3), 879-890. <http://dx.doi.org/10.13031/trans.58.11033>
- Boac, J. M., Bhadra, R., Casada, M. E., Thompson, S. A., Turner, A. P., Montross, M. D., ... Maghirang, R. G. (2015). Stored grain pack factors for wheat: Comparison of three methods to field measurements. *Trans. ASABE*, 58(4), 1089-1101. <http://dx.doi.org/10.13031/trans.58.10898>
- Casada, M. E., & Armstrong, P. R. (2009). Wheat moisture measurement with a fringing field capacitive sensor. *Trans. ASABE*, 52(5), 1785-1791. <http://dx.doi.org/10.13031/2013.29119>
- Chang, C. S., Converse, H. H., & Martin, C. R. (1983). Bulk properties of grain as affected by self-propelled rotational type grain spreaders. *Trans. ASABE*, 26(5), 1543-1550. [10.13031/2013.34167](http://dx.doi.org/10.13031/2013.34167)
- Chang, C. S., Shackelford, L. E., Lai, F. S., Martin, C. R., & Miller, B. S. (1981). Bulk properties of corn as affected by multiple-point grain spreaders. *Trans. ASAE*, 24(6), 1632-1636. <http://dx.doi.org/10.13031/2013.34504>
- CurveExpert Professional Software, version 2.0.3. 2013. Developer: Daniel G. Hyams. Available at; <https://www.curveexpert.net/>
- Fang, Y. (2011). Asymptotic equivalence between cross-validations and Akaike information criteria in mixed-effects models. *J. Data Sci.*, 9(1), 15-21.
- Janssen, H. A. (1895). Versuche uber getreidedruck in silozellen. *Zeitschr. d. Vereines deutscher Ingenieure*, 39(35), 1045-1049.
- Loewer Jr., O. J., Ross, I. J., Kratzer, D. D., & Walker, J. N. (1977). Properties of ground shelled corn as related to forces in bulk storage structures. *Trans. ASAE*, 20(1), 155-156. <http://dx.doi.org/10.13031/2013.35512>
- Malm, J. K., & Backer, L. F. (1985). Compaction factors for six crops. *Trans. ASAE*, 28(5), 1634-1636. <http://dx.doi.org/10.13031/2013.32489>
- Matz S A 1991 Wheat. In: The Chemistry and Technology of Cereals as Food and Feed. Van Nostrand Reinhold, New York, USA, pp 1-61.
- McNeill, S. G., Montross, M. D., Thompson, S. A., Ross, I. J., & Bridges, T. C. (2008). Technical note: Packing factors of feed products in storage structures. *Appl. Eng. Agric.*, 24(5), 625-630. <http://dx.doi.org/10.13031/2013.25260>
- Milani, H. P., Bucklin, R. A., Teixeira, A. A., & Kabeli, H. V. (2000). Soybean compressibility and bulk density. *Trans. ASAE*, 43(6), 1789-1793. <http://dx.doi.org/10.13031/2013.3082>
- Steel, R. G. D., & Torrie, J. H. (1980). *Principles and procedures of statistics: A biometrical approach* (2nd ed.). New York, NY: McGraw-Hill.
- Thompson, S. A., & Ross, I. J. (1983). Compressibility and frictional coefficients of wheat. *Trans. ASAE*, 26(4), 1171-1176. <http://dx.doi.org/10.13031/2013.34099>
- Thompson, S. A., McNeill, S. G., Ross, I. J., & Bridges, T. C. (1987). Packing factors of whole grains in storage structures. *Appl. Eng. Agric.*, 3(2), 215-221. <http://dx.doi.org/10.13031/2013.26677>
- USDA-GIPSA. (2009). Inspecting grain: Practical procedures for grain handlers. Washington, DC: USDA Grain Inspection, Packers and Stockyards Administration. Federal Grain Inspection Service. Retrieved from http://www.gipsa.usda.gov/Publications/pub_fgis.html#hb